

PATENT APPLICATION

of

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for a

METHOD AND APPARATUS FOR MODULATION USING AN AT LEAST  
FOUR-DIMENSIONAL SIGNAL CONSTELLATION

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FOUR-DIMENSIONAL SIGNAL CONSTELLATION

TECHNICAL FIELD

5 The present invention is related to the communication of  
digital information, and more particularly to signal  
constellations used by digital communications systems to  
encode groups of bits as symbols.

BACKGROUND ART

10 According to the prior art, in a digital communication  
system, sets of consecutive bits in a bit stream are mapped to  
symbols, sometimes considered to be complex symbols having a  
real part and an imaginary part, with the real part used to  
modulate an in-phase carrier signal and the imaginary part  
used to modulate a quadrature-phase carrier signal. The data  
15 rate of such a digital communication system depends on, among  
other factors, the number of bits represented by each symbol.  
The bit error rate, depends on, among other factors, the  
distance, in an abstract mathematical sense, between any two  
points in the set of symbols used to represent/encode the bit  
20 stream. The set of symbols can be indicated as a so-called  
signal constellation (or symbol constellation), which is a  
representation showing how the correspondence between each  
symbol and a respective sequence of bits, the representation  
sometimes being provided as a plot of the symbols as points in  
25 a usually two-dimensional space. An example of a signal  
constellation is shown in Fig. 1A for quadrature phase shift  
keying (QPSK) modulation, the signal constellation there  
showing that the bit sequence 00 is mapped to the symbol  
 $\sqrt{P} + 0j$ , the bit sequence 01 is mapped to the symbol  $0 + j\sqrt{P}$ ,  
30 and so on, where P is the power used by the digital  
communication system in transmitting one symbol.

As mentioned above, the bit error rate of a digital communication system depends on the distance properties of the signal constellation being used. In the case of QPSK, using as a measure of distance the Euclidean between points in the abstract signal constellation space, the minimum distance between any two points in the signal constellation is, as can be seen from Fig. 1A,

$$D = \sqrt{2P},$$

where, as mentioned above,  $P$  is the signal power used to transmit one symbol, i.e. the power used during one symbol period.

Another representation of the QPSK signal constellation for QPSK modulation, a representation equivalent to the representation shown in Fig. 1A, is shown in Fig. 1B. The Fig. 1B representation indicates that for the bit string corresponding to  $k=3$  (i.e. for the bit sequence 11), the QPSK symbol is  $-R+0j$  (where  $R=P$ , as indicated in Fig. 1A).

To increase the bit rate it is possible to use so-called MSK modulation with  $M>4$ . For example, 8PSK modulation transmits 3 bits per symbol. Such approaches to improving system performance by improving the bit rate also use two-dimensional signal constellations, like QPSK modulation, but because the signal constellation space is more densely packed than for systems encoding fewer bits per symbol, the smallest distance between any two points for MSK signal constellations (with  $M>4$ ) is smaller, and so the bit error rate worsens.

Another approach has been to use higher-dimensional signal constellations. The prior art teaches using signal points carved from a higher dimensional lattice/ trellis code. However, the distance properties for such constellations are not optimal, and an implementation of systems using such signal constellations can be complicated.

What is needed is a higher-dimensional signal constellation not based on lattice/ trellis codes, and ideally one with distance properties that are superior to those of signal constellations carved from such codes.

5 DISCLOSURE OF THE INVENTION

Accordingly, in a first aspect of the invention, a digital communication system is provided having a symbol generator and a modulator, the symbol generator for translating a bit stream into a symbol stream based on a 10 predetermined signal constellation, each symbol in the symbol stream representing a predetermined even number of consecutive bits in the bit stream, the modulator using a predetermined modulation scheme to modulate a carrier signal with the symbol stream so as to provide a modulated carrier signal, 15 characterized in that the signal constellation has a dimensionality that is at least four and is an integral multiple of two, and that each symbol of the signal constellation corresponds to an ordered set of at least two sets of two or more numbers, and further characterized in that 20 for each of the at least four-dimensional symbols, the modulator modulates the carrier signal using in turn each of the at least two corresponding sets of two or more numbers.

In accord with the first aspect of the invention, each symbol of the signal constellation may be located in the signal constellation so as to be separated from any other symbol by at least a distance of  $a^5 p^{1/2} / b$ , where  $a=2^{1/4}$  and  $b=(1+2^{1/2})^{1/2}$  and  $P$  is the power radiated in transmitting one symbol.

In a second aspect of the invention, a method is provided by which a digital communication system transmits a bit stream, the digital communication system having a symbol generator and a modulator, the symbol generator for translating the bit stream into a symbol stream based on a 30

predetermined signal constellation, each symbol in the symbol stream representing a predetermined even number of consecutive bits in the bit stream, the modulator using a predetermined modulation scheme to modulate a carrier signal with the symbol stream so as to provide a modulated carrier signal, characterized in that the signal constellation has a dimensionality that is at least four and is an integral multiple of two, and that each symbol of the signal constellation corresponds to an ordered set of at least two sets of two or more numbers, and further characterized in that for each of the at least four-dimensional symbols, the modulator modulates the carrier signal using in turn each of the at least two corresponding sets of two or more numbers.

In accord with the second aspect of the invention, each symbol of the signal constellation may be located in the signal constellation so as to be separated from any other symbol by at least a distance of  $a^5 P^{1/2} / b$ , where  $a=2^{1/4}$  and  $b=(1+2^{1/2})^{1/2}$  and  $P$  is the power radiated in transmitting one symbol.

#### 20 BRIEF DESCRIPTION OF THE DRAWINGS

The above and other objects, features and advantages of the invention will become apparent from a consideration of the subsequent detailed description presented in connection with accompanying drawings, in which:

25 Fig. 1 is the signal constellation for QPSK modulation;

Fig. 1B is another representation of the signal constellation for QPSK modulation;

30 Fig. 2 is a block diagram/flow diagram of components of a digital communication system according to the present invention, showing the use of a four-dimensional signal constellation; and

Fig. 3 is a representation of the four-dimensional signal constellation used in the digital communication for which some elements are shown in Fig. 2.

BEST MODE FOR CARRYING OUT THE INVENTION

5 The invention is described below for an application in which a four-dimensional signal constellation is used. It should be understood, however, that the invention encompasses higher-dimensional signal constellations as well, such as for example a six-dimensional signal constellation or any other  
10 higher, even-dimensional constellation. Further, although the invention is described for a particular four-dimensional signal constellation, any orthogonal transformation (i.e. rotation) of the signal constellation is also encompassed by the invention.

15 An approach that can be used to determine a  $(d+1)$ -dimensional spherical signal constellation is as follows. (Although we always want to end up with an even-dimensional constellation, the construction proceeds inductively, and as a by-product we generate also odd-dimensional constellations.)  
20 Begin with a  $d$ -dimensional signal constellation, which will contain  $2^d$ -points. Then generate a  $(d+1)$  dimensional spherical signal constellation, with  $2^{d+1}$ -points on the  $(d+1)$ -dimensional sphere, by constructing the constellation that is the union of the two disjoint sets A and B, where B is the  
25 image of A under isometric transformation UP, i.e.  $B=UP(A)$ , in which P is the reflection with respect to the plane  $x_{d+1}=0$ , and U is an orthogonal transformation operating only on the coordinates  $(x_1, \dots, x_d)$ . The set A is the optimal constellation on the  $d$ -dimensional sphere, which is now a subset of the  $d+1$ -dimensional sphere. This  $d$ -dimensional sphere is an  
30 intersection of the  $d+1$ -dimensional sphere and the plane  $x_{d+1}=+h$ . The sets A and B are discrete sets on the surface

of a  $d+1$ -dimensional sphere, i.e. on the surfaces/ planes  $x_{d+1} = +h$  and  $x_{d+1} = -h$ , respectively. The intersection of the planes  $x_{d+1} = \pm h$  and the  $(d+1)$ -dimensional sphere is a  $d$ -dimensional sphere with radius  $\sqrt{R^2 - h^2}$ . So the sets A and B are eventually on the  $d$ -dimensional sphere. Next take for A (and hence for B) the optimal  $d$ -dimensional constellation. What remains are some free parameters  $h$  and the elements of the transformation U. These have to be determined in such a manner that the minimum distance between the points is maximized. As described above, in the invention this scheme is carried out explicitly for a 4-dimensional constellation.

Referring now to Figs. 2 and 3, a digital communication system 20 according to the invention is shown as including a symbol generator 21 for translating a bit stream into a symbol stream, i.e. into a stream of symbols, in which each symbol represents four bits, the translation being performed in accord with a predetermined signal constellation 30 (Fig. 3). For example, bit sequence 0110, which in decimal is the value  $k = 6$ , corresponds to the four-dimensional symbol having coordinates  $(x_1, x_2, x_3, x_4) = (-aR/b, 0, -R/a^2b, +R/a^2b)$  where  $a=2^{1/4}$ ,  $b=(1+2^{1/2})^{1/2}$  and  $R=(2P)^{1/2}$ , in which  $2P$  is the power radiated in transmitting one four-dimensional symbol.

Now referring only to Fig. 2, the invention also includes a modulator 22 that uses the symbol stream provided by the symbol generator 21 to modulate a carrier signal according to a predetermined two-dimensional modulation scheme, such as quadrature amplitude modulation (QAM), so as to provide a modulated carrier signal, and does so by modulating the carrier with each symbol in two steps, a first step in which the first two coordinates  $x_1$   $x_2$  of the four-dimensional symbol are used to modulate the carrier according to the predetermined two-dimensional modulation scheme, and a second step in which the next two coordinates  $x_3$   $x_4$  are used to

modulate the carrier signal according to the same two-dimensional modulation scheme. For example, for an implementation using QAM, the first two coordinates  $x_1$   $x_2$  are taken to correspond to a first complex number  $x_1+jx_2$ , or more generally and equivalently, to a first pair of numbers  $(x_1, x_2)$ , which is then used as the input to a QAM modulator, and the next two coordinates  $x_3$   $x_4$  are taken to correspond to a second complex number  $x_3+jx_4$ , or more generally and equivalently, to a second pair of numbers  $(x_3, x_4)$ , which is then used as the input to the same QAM modulator. For an implementation using QPSK, the same correspondences would be made, but a QPSK modulator would be used. The same idea for transmission could be used for 16 QAM (four bits per symbol), i.e. one could have an eight-dimensional signal constellation, and transmit each symbol in two parts using 16 QAM for each part. Or one could transmit each symbol of an eight-dimensional signal constellation in four parts, using QAM (or, equivalently, 4 QAM) or QPSK for each part. (Note that the notation QAM is used here to indicate a modulation scheme encoding two bits per symbol, and so providing 4 symbols. The notation KQAM is used to indicate a modulation scheme encoding  $\log_2(K)$  bits per symbol, and so providing K symbols. Thus, according to the notation here, QAM is equivalent to 4QAM.)

Additionally, instead of using two modulators for each of which a symbol represents 2 bits, such as QAM modulators, one could use two modulators in each of which each symbol represents 3 bits, such as 8QPSK modulators or 8QAM modulators. Thus, two sets of three numbers would be transmitted instead of two sets of two numbers, as in QAM or 4PSK. Referring back to Fig. 3, it can be seen that the smallest distance between any two symbols in the signal constellation 30 of the invention is  $a^5b^{-1}P^{1/2}$ , compared to  $a^2P^{1/2}$  for QPSK.

Thus, in the present invention, a four-dimensional symbol is transmitted in two parts (and a six-dimensional symbol would be transmitted in three parts, and so on, or an eight-dimensional symbol could be transmitted in two parts using a 5 modulation scheme that transmits four bits per symbol, and so on) but because the distance properties of the four-dimensional signal constellation are improved over those of the two-dimensional signal constellation used in the two-dimensional modulation scheme according to the prior art, the 10 bit error rate is improved by the present invention (although the bit rate is unchanged from what it is in the prior art).

*Scope of the Invention*

It is to be understood that the above-described arrangements are only illustrative of the application of the 15 principles of the present invention. Numerous modifications and alternative arrangements may be devised by those skilled in the art without departing from the scope of the present invention, and the appended claims are intended to cover such modifications and arrangements.